

EXPERIMENTAL AND THEORETICAL INVESTIGATION OF HICROWAVE AND HILLIMETER WAVE RADIATION PRON HOLLOW, ROTATING, ELECTRON BEAMS  7. AUTHOR(a) W. W. Destler E. L. Weiler C. D. Striffler  8. CONVARCY OR GRANT HUMBER(a) APOSR 78-3690  8. PERFORMING ORGANIZATION NAME AND ADDRESS University of Maryland Electrical Engineering Department College Park, MD 20742  10. CONTROLLING OFFICE WAME AND ADDRESS ALT FORCE Office of Scientific Research/NP Building 410 Bolling AFB DC 20332  14. MONITORING AGENCY NAME & ADDRESS(II dillorent from Controlling Office)  15. SECURITY CLASS. (of this report) UNCLASSIFIED  16. DISTRIBUTION STATEMENT (of this Report)  DTC  16. DISTRIBUTION STATEMENT (of this Report)		
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18. SUPPLEMENTARY NOTES

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

39. ABSTRACT (Continue on reverse side if necessary and identify by block number)
During this period this effort has explored the scaling of the regative mass instability to regimes associated with smaller plasmas and short wavelengths for the plasma-produced radiation. An experimental apparatus for these studies is near completion. The nonlinear electromagnetic interaction between the collective/bunches of electrons and the radiation field has been formulated in an attempt to derive the efficiency of the production of radiation. In addition the Dragon electron beam source is currently being improved for future radiation production experiments based on the negative mass instability. (Over)

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Experimental efforts at high powers have resulted in the enhancement of radiation at a single frequency. This last effort has utilized a "double-magnetron cavity" to enhance the radiation power in Ka band at 26 and 41GHz.

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# AFOSR-TR- 82-0532

EXPERIMENTAL AND THEORETICAL INVESTIGATION OF MICROWAVE AND MILLIMETER WAVE RADIATION FROM HOLLOW, ROTATING, ELECTRON BEAMS

Contract No. AFOSR-78-3690

PROGRESS REPORT

For the Period December 1, through November 30, 1981

Submitted to

Air Force Office of Scientific Research

Prepared by

Charged Particle Beam Research Group Electrical Engineering Department University of Maryland College Park, Maryland 20742

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#### PROGRESS REPORT

SUBMITTED TO:

Air Force Office of Scientific Research

SUBMITTED BY:

Electrical Engineering Department

University of Maryland College Park, MD 20742

GRANT NUMBER:

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PRINCIPAL INVESTIGATORS:

William W. Destler, Associate Professor Charles D. Striffler, Associate Professor

Electrical Engineering Department

TITLE OF RESEARCH PROJECT:

"Experimental and Theoretical Investigation of Microwave Radiation from Hollow, Rotating,

Electron Beams"

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MATTHEW J. KERPER
Chief, Technical Information Division

Interim Progress Report

for the period December 1, 4199 to November 30, 1981

### I. Introduction

The technical summary is divided into three parts, one describing the equipment status, the second the experimental program, and the third outlines the theoretical studies that have been initiated. A list of publications and presentations resulting from this work may be found in Appendix B.

#### II. Experimental Apparatus and Equipment

During the past year, a 12-18 GHz detection system has been constructed and calibrated. This system now gives us detection capability in the ranges 7-12 GHz, 11-18 GHz, 24-40 GHz, and 60-90 GHz. Equipment in the 18-26 GHz band is currently being acquired.

Several new experimental subsystems have been constructed, the most important of which are n=20 and n=40 multiresonator outer conducting boundaries. These systems, and the reasons for their construction, are outlined in the next section.

#### III. Experimental Research

The experimental research program has centered around two general areas:

(1) the characterization and optimization of the broadband radiation observed when a hollow, nonneutral, rotating E-layer propagates inside a simple cylin drical or coaxial conducting boundary system, and (2) the use of carefully tailored conducting boundary configurations and/or a preloaded azimuthal density structure on the beam to induce radiation at specific frequencies. The

results of these studies up to the beginning of the period covered by this progress report are summarized in two papers enclosed in Appendix C ("Intense Microwave Radiation from a Non-Neutral, Rotating E-layer," <u>Journal of Applied Physics</u>, May 1981, and "High Power Microwave Generation from a Rotating E-layer in a Magnetron-type Waveguide," <u>Applied Physics Letters</u>, April 1981). The major results of this work obtained during the current grant period are:

A. Radiation from Rotating E-layers Propagating in Simple Cylindrical or Coaxial Conducting Boundary Systems

- (1) The radiation has been measured in the 11-18 GHz band, and as expected from previous data obtained in the 7-12 GHz band, radiated power is detected at various harmonics of the electron cyclotron frequency. This result is in good qualitative agreement with theory. A typical radiated power spectrum obtained on a single shot (and including all three bands) is shown in Figure 1. Typical electron beam parameters downstream of the cusp transition are 2 MeV, 2 kA, 5 ns. The relatively high radiated power in the 24-40 GHz band may be due to the onset of the TM modes, which do not occur theoretically until about 18 GHz.
- (2) Radiated power over all bands is not a strong function of magnetic field in the range 1000-1400 gauss. Above 1400 gauss, the beam electrons are reflected at the cusp transition, and no radiation is observed because there is no rotating beam current on the downstream side of the cusp. Below 1000 gauss, radiation falls off rapidly as the magnetic field is decreased. It is believed that at these magnetic field values the electron cyclotron frequency is reduced to the

point where there is no resonance between the beam modes and the waveguide modes. In addition, the electron beam density is also reduced due to a decrease in the axial compression of the beam due to the cusp.

- B. Radiation from Rotating E-layers Propagating in Magnetrontype (Multiresonator) Boundary Systems
- (1) n = 20 and n = 40 multiresonator boundary systems have been constructed and tested. Substantial peaking of the radiation spectrum at about  $n\omega_{ce}$  is observed in these systems, and a typical Ka band spectrum for the n = 40 boundary is shown in Figure 2 (along with a spectrum obtained when the multiresonator boundary is replaced by a simple cylindrical boundary of the same outer dimension).
- (2) For these systems, substantial power is also observed at about 10 GHz. As this frequency corresponds to a half wavelength equal to the distance between the beam and the outer conducting wall, it is possible that the radiation results from a transfer of energy from beam modes to the modes of the resonators. Further studies of this phenomena are currently in progress.
- (3) The radiation is strongly peaked at values of axial magnetic field somewhat below the cusp cutoff value, as shown in Figure 3. This peaking is much stronger than that observed when a simple cylindrical boundary is used.

In addition to these studies, we have performed initial experimental design studies on an experiment to investigate the interaction of a rotating electron beam with a dielectric-lined outer conducting boundary (an experiment to be performed in collaboration with Professor John Walsh's group at Dartmouth College) and we have begun to investigate the feasibility of constructing a table-top rotating beam experiment for microwave and millimeter wave generation experiments. These efforts will be outlined in more detail in the summary of proposed research for the new grant period.

## IV. Theoretical Research

The theoretical research program has centered around two general areas;

(A) the radiated power spectrum at the end of a cylindrical drift tube due to a harmonically modulated electron ring, and (B) the waveguide modes in a magnetron-type conducting boundary. The first topic has been completed and its results are presented below. The second topic is ongoing and will be discussed in the section on "Research Goals." Recall that we completed a linear stability analysis of an E Ring in a hollow drift tube and of a long E Layer in a coaxial drift tube during the previous year. The results of the E Layer studies are presented in the enclosed paper in Appendix C. These results showed qualitative agreement with the experimentally radiated spectrum.

As a preliminary to the study of the efficiency of rotating beams for conversion of beam kinetic energy into radiated energy, we have calculated the radiated power spectrum out the end of a hollow drift tube due to a stationary, harmonically modulated E Ring. The geometry for this analysis is shown in Figure 4. As shown, the ring is symmetrically located along the axis of a cylindrical drift tube of radius Rw at a distance Zo from the closed end of the tube. The ring has a mean radius R, radial thickness  $\Delta R$ , axial length  $\Delta Z$ , a mean azimuthal

velocity  $V\phi$  and uniform charge density  $\rho_0$ . The ring is assumed to have a finite pulse width designated by  $T_w$ . As a function of these beam parameters, we have calculated the power radiated out the open end of the drift tube for the following harmonically modulated charge density;

$$\rho(r,q,z,t) = \left\{ \rho_0(r,z) + \sum_{l,\omega} \rho_i(r,z) e^{i(lp-\omega t)} \right\} f_{T_{w}}(t)$$

and consistent current density  $J_{\rho}(r,\rho,z,t) = V_{\rho}\rho(r,\rho,z,t)$ , where  $\rho_{o}$  is the mean charge density and  $\rho_{r}$ , the modulated amplitude. The pulse profile  $f_{T_{w}}(t)$  is chosen as

$$f_{w}(t) = \Theta\left[t + T_{w}\right] - \Theta\left[t - T_{w}\right],$$

a unit pulse of width  $T_w$ , and we choose  $\rho$  (r,z) as a uniform modulated charge over the cross section of the beam. Maxwells Equations can be decomposed into TE and TM modes and each analyzed separately. We have first computed the Greens Function in space and time for each mode and thus by appropriate integrations can calculate a radiated energy density,  $\mathcal{E}_{L,N}$ . For the TM mode we find

and for the TE mode

$$E_{TE_{L,n}} = \frac{e^{2}N_{e}^{2}\omega\beta_{\varphi}^{2}}{4T^{2}E_{0}} \frac{\sin^{2}k_{z}}{k_{z}^{2}\Delta z^{2}} \times \left[ \int_{R-\Delta R/z}^{R+\Delta R/z} (k_{z}'r) \frac{\sin Tw(\omega-\omega)k_{z}}{\omega-\omega'} + \int_{R-\Delta R/z}^{R+\Delta R/z} (k_{z}'r) \frac{\sin Tw(\omega-\omega)k_{z}}{\omega-\omega'} + \int_{R-\Delta R/z}^{R+\Delta R/z} \int_{R-\Delta R/z}^{R+\Delta R/z} \int_{R-\Delta R/z}^{R+\Delta R/z} \left[ \int_{R-\Delta R/z}^{R+\Delta R/z} \int_{R-\Delta$$

where  $K_2^2 = \omega^2/C^2 - K_n^2(TM)$ ,  $K_2^2 = \omega^2/C^2 - K_n'^2(TE)$ ,  $J_L(K_L R_W) = 0$ ,  $K_R = \int L L R_W$ ,  $J_L(K_L R_W) = 0$ ,  $K_R = \int L L R_W$ , and  $N_L$  is the number of particles in the perturbed L mode. In each case we can define an average radiated power  $P_{LR} = \mathcal{E}_{LR}/T_W$ . Typical results are shown in Figures 5 - 9. In each graph we

have plotted average radiated power versus frequency. Fixed parameters are  $N_{\ell} = 10^{12}$  and  $\beta_{\phi} = .986(\gamma=6)$ . Figure 5 is the radiated spectrum for a ring filament of infinite pulse length and no end plate. The radiated frequencies are at  $\ell \omega_{R} = \ell V \phi / R$  and we see that the n = 1, 2 and 3 radial modes can radiate in the frequency regime considered. The TE modes set in at about 6 GHz and the TM modes at about 20 GHz. Figure 6 shows the effects of an end plate. Some modes constructively interfere and others cancel. In Figure 7, the effects of finite axial length of the ring are shown. In Figures 8 and 9 the effects of finite pulse width and finite radial thickness are shown for an  $\mathcal{L}$  = 40 TM mode. In Figure 8, the effects of only finite pulse width are shown and we see the expected broadening of the radiated spectrum about the L = 40 frequency. In Figure 9 we add on the effects of finite radial width which because of our choice of beam model produces similar effects as does finite pulse width. When all these effects are put together, the discrete spectrum of Figure 5 becomes a rather comtinuous spectrum in the frequency regime of the TM modes, i.e., greater than about 20 GHz, yet these effects at lower frequencies, i.e., in the TE mode regime, are less dramatic and the spectrum remains rather discrete. These theoretical results are in very good agreement with respect to form with those of the measured radiated spectrum in X and Ka bands.

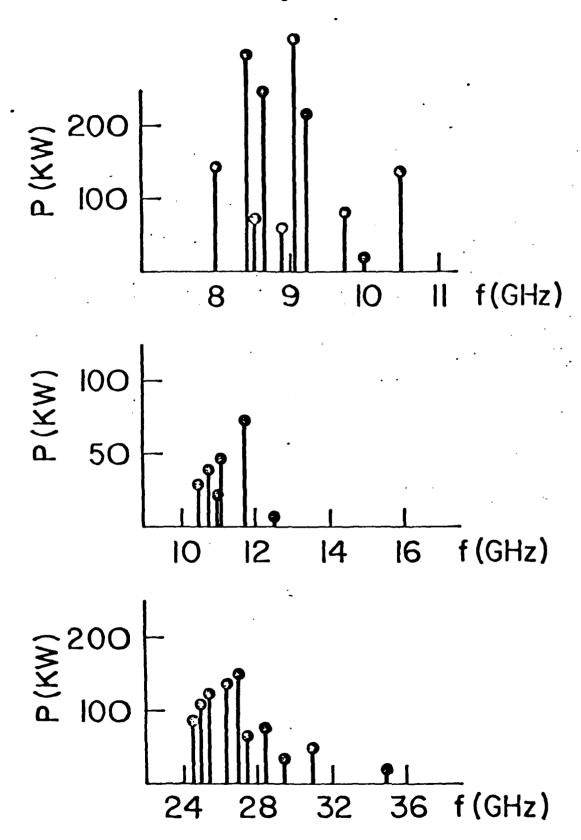


Figure 1. Typical radiated power spectrum for three different detection bands (X, Ku, Ka) produced by a rotating electron beam in a cylindrical drift tube.

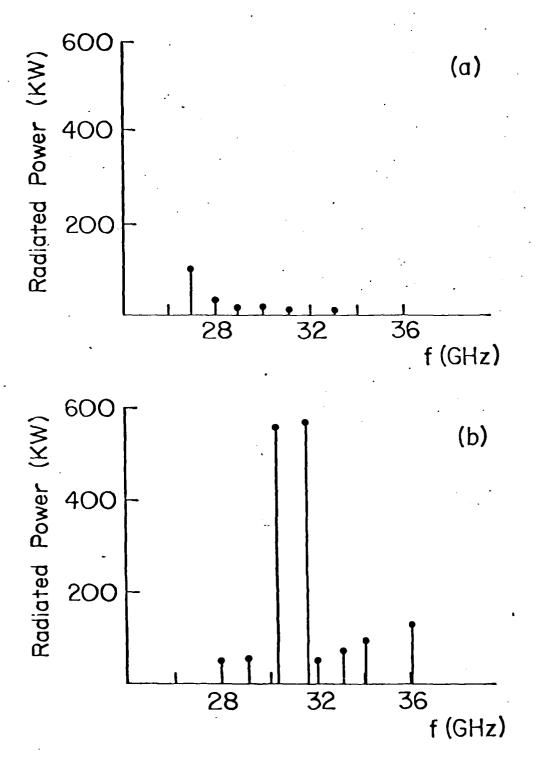


Figure 2. Typical radiated power spectra in Ka band for (a) a rotating beam in a cylindrical drift tube, and (b) a rotating beam in a n = 40 magnetron-type outer conducting boundary.

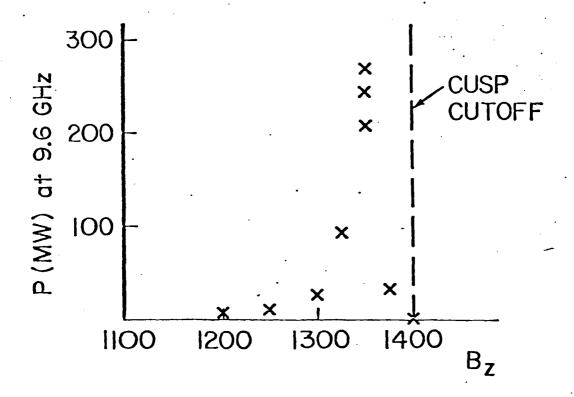


Figure 3. Radiated power at 9.6 GHz as a function of applied axial magnetic field for a rotating beam in a n = 12 magnetron type outer conducting boundary.

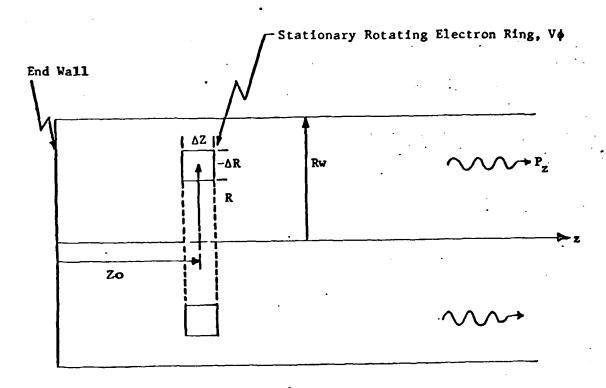
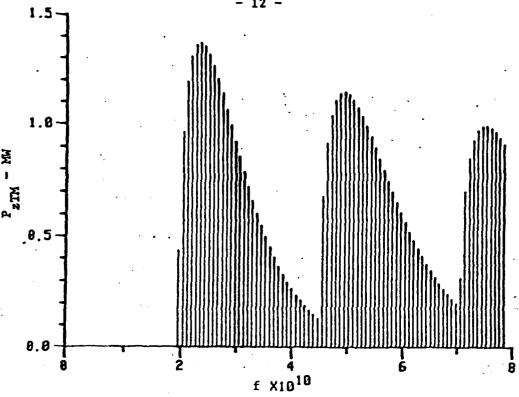


Figure 4: 'Geometry of model for radiation analysis.



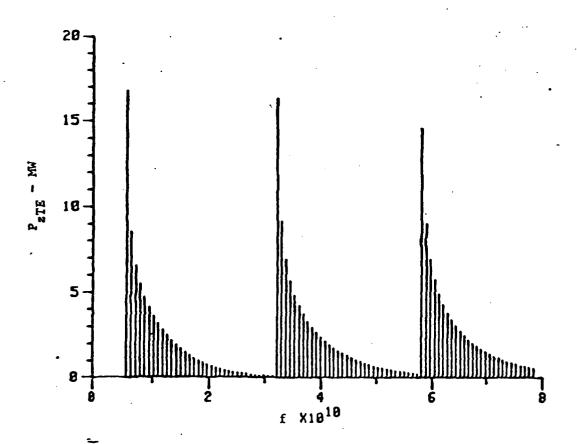
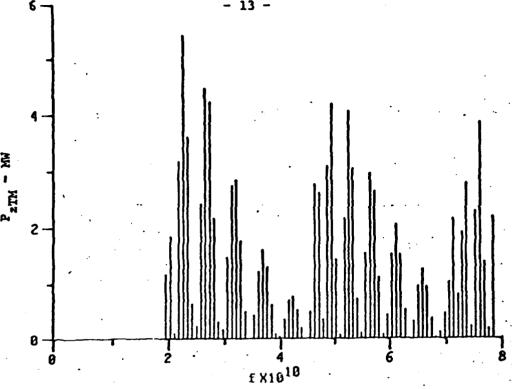


Figure 5: Power results for TM & TE modes, no end plate, infinite pulse length,  $\Delta Z$  &  $\Delta R$  = 0,  $N_{L}$  =  $10^{12}$ ,  $\beta_{P}$  = .986.



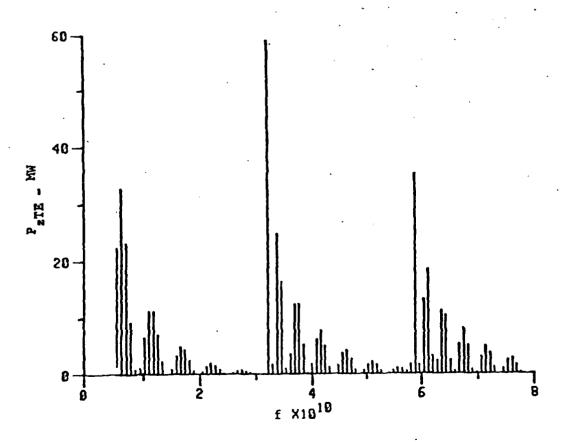
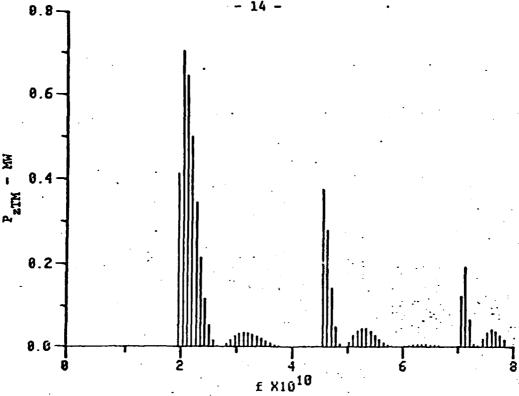


Figure 6: Power results for TM & TE modes, with end plate,  $T_W$   $\Delta Z$  &  $\Delta R$  = 0,  $N_L$  =  $10^{12}$ ,  $\beta_{\phi}$  = .986,  $Z_O$  = 5 cm.



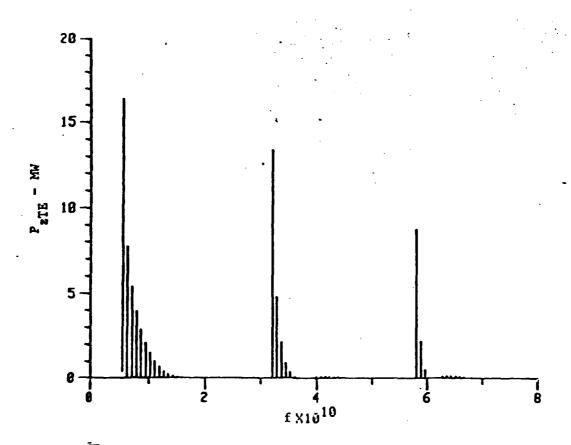
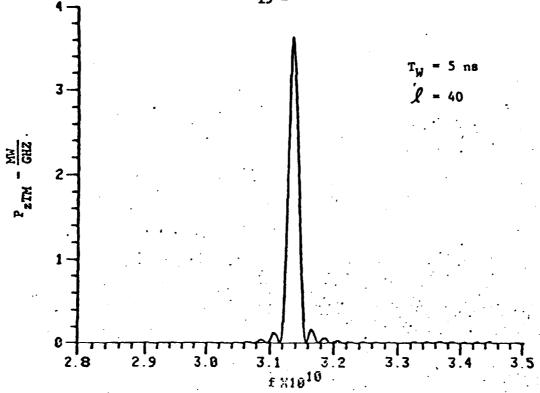


Figure 7: Power results for TM & TE modes, no end plate,  $T_W$   $\Delta Z = 4 \text{ cm}, \ \Delta R = 0, \ N_Z = 10^{12}, \ \beta_P = .986.$ 





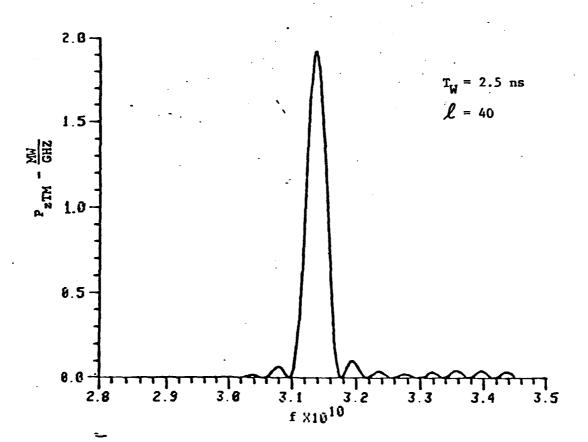
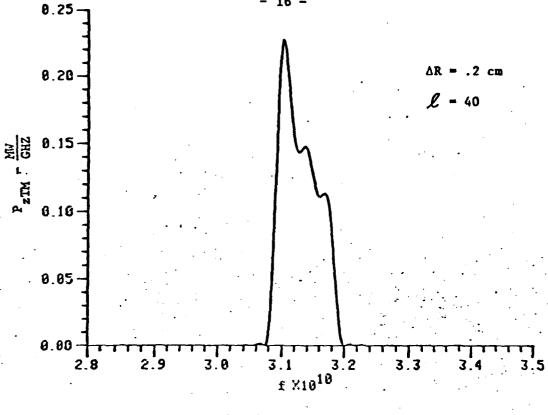


Figure 8: Power results for TM mode with finite pulse length,  $\Delta Z = 0$ ,  $\Delta R = 0$ ,  $N_{\ell} = 10^{-2}$ ,  $\beta_{\ell} = .986$ , no end plate.





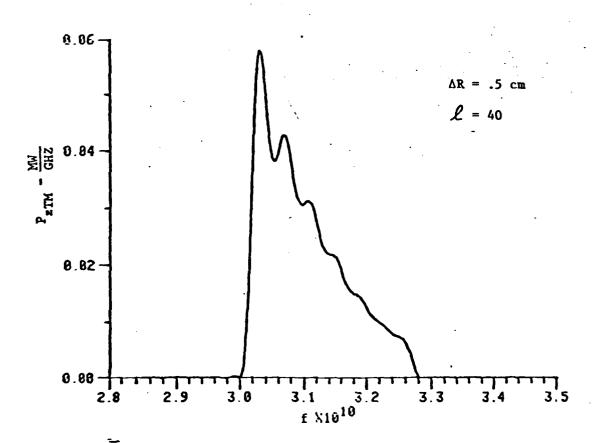


Figure 9: Power result for TM mode, no end plate,  $T_W = 5$  ns,  $\Delta Z = 0$ ,

#### APPENDIX B

List of Publications and Presentations Resulting from this Work

- 1. "Experimental Study of Intense Microwave Generation by the Negative Mass Instability," W. W. Destler, W. Namkung, and R. L. Weiler, Bull. Am. Phys. Soc. 24, 1068 (October 1979).
- 2. "Theoretical Study of Microwave Generation from a Rotating E-Layer-Co-axial Waveguide System," W. Namkung, H. Romero, and C. D. Striffler, Bull. Am. Phys. Soc. 24, 1068 (October 1979).
- 3. "Negative Mass Instability of a Relativistic E Ring in a Hollow Waveguide,"
  T. F. Wang and C. D. Striffler, Bull. Am. Phys. Soc. 24, 1068 (October 1980).
- 4. "High Power Microwave Generation from an Intense Rotating Electron Beam," W. W. Destler, C. D. Striffler, W. Namkung, H. Romero, and R. Weiler, 1980 IEEE Int. Conf. on Plasma Science, Madison, Wisconsin (May 19-21, 1980).
- 5. "High Power Microwave Generation from a Cusp-Injected Magnetron," W. W. Destler, R. Kulkarni, C. D. Striffler, and R. L. Weiler, Bull. Am. Phys. Soc. II, 25, 886 (1981).
- 6. "High Power Microwave Generation from a Rotating E-Layer in a Magnetrontype Waveguide," W. W. Destler, R. L. Weiler, and C. D. Striffler, Appl. Phys. Lett. 38, 570 (1981).
- 7. "High Power Microwave Generation from a Rotating E-Layer in Various Conducting Wall Systems," W. W. Destler, R. Kulkarni, C. D. Striffler, and R. Weiler, 1981 IEEE Int. Conf. on Plasma Science, Santa Fe, New Mexico (May 18-20, 1981).
- 8. "Intense Microwave Generation from a Non-Neutral Rotating E Layer," W. W. Destler, H. Romero, C. D. Striffler, R. L. Weiler, and W. Namkung, J. of Appl. Phys. (to be published).

# APPENDIX C

Copies of Papers Published and Abstracts of Papers Presented

# Intense microwave generation from a non-neutral rotating E layer

W. W. Destler, H. Romero, C. D. Striffler, R. L. Weiler, and W. Namkung Electrical Engineering Department, University of Maryland, College Park, Maryland 20742

(Received 28 July 1980; accepted for publication 10 November 1980)

The radiation produced by a hollow, non-neutral, rotating, relativistic E layer propagating inside a coaxial cylindrical drift tube has been investigated theoretically and experimentally. The measured radiation spectrum is very broadband in agreement with theory, though a shift in the spectrum can be achieved by a preloaded azimuthal density structure.

PACS numbers: 52.80.Vp, 52.60. + h,

#### I. INTRODUCTION

The production of very-high-power bursts of microwave radiation by coupling the output of high-current relativistic electron accelerators to conventional microwave devices (Klystrons, Backward Wave Oscillators, and Magnetrons) has been reported by several groups during the past few years. 1-5 Many of these experiments have reported conversion efficiencies of electron beam power to microwave power comparable to those achieved in conventional devices working at much lower power levels. The successful application of high-power electron accelerators for the efficient generation of microwave radiation has led to the investigation of several new concepts aimed at intense microwave and millimeter wave production. These new concepts are designed to produce radiation at frequencies attractive for such diverse applications as plasma heating and atmospheric propagation. These new ideas include gyrotrons,6 free-electron lasers, and radiation from nonneutral rotating E layers, the subject of this report.

The loss of electron energy to radiation in rotating electron rings and E layers has been reported by several groups during the past decade, 10-12 usually as part of studies aimed at reducing this radiated energy in order to maintain beam quality. In the work reported here, theory and experiment undertaken with the goal of characterizing and maximizing the microwave radiation from such rotating E layers is reported. Initial studies of the microwave radiation from a rotating E layer were reported by Granatstein et al., 8 and a theoretical analysis of the resonant interaction between beam modes and the TE and TM modes of the vacuum drift chamber in such a system were reported by Sprangle. 13 A more complete experimental study of this radiation production (and its suppression when so desired) was reported by Destler et al.,9 and subsequent theoretical analysis has been provided by several groups. 14,15

In Fig. 1, a schematic is shown of the experimental system that is used in our studies of microwave generation. The diode is composed of a thin annular cathode of mean radius 6 cm and an anode plate through which the beam passes into the cusped magnetic field. The nominal diode properties are 2-MV, 20-30-kA, and 20-30-ns pulse width. The cusped magnetic field is formed by oppositely driven current coils and an iron plate. A typical axial magnetic field profile is shown in Fig. 1 where we see the field is essentially uniform in a region immediately downstream of the cusp. After pas-

sage through the cusp, the hollow rotating E layer has nominal properties of 2-MeV particle energy, 1-2-kA, and 5-10-ns pulse width. The beam is radially thin and axially long because the magnetic field setting is generally 50 G or so below the cutoff magnetic field. Since the beam is fairly tenuous, the rotating azimuthal velocity is that of axis-encircling cyclotron motion,

$$v_{\phi 0} = r_0 \omega_c = r_0 e B_0 / m \gamma_0 \tag{1}$$

where  $r_0$  is the cathode radius,  $B_0$  the uniform downstream magnetic field, and  $\gamma_0$  the relativistic mass ratio, i.e.,  $mc^2(\gamma_0-1)=\mathrm{eV}_0{\simeq}2$  MeV. The axial velocity depends on the magnetic field setting, and for balanced cusped fields is given by

$$v_{z0}/c = \left[ (\gamma_0^2 - 1)/\gamma_0^2 - (r_0 e B_0 / m c \gamma_0)^2 \right]^{1/2}, \tag{2}$$

from which we see a "cutoff" field of

$$B_{0c} = (mc/er_0)(\gamma_0^2 - 1)^{1/2}.$$
 (3)

The post cusp hollow beam propagates down a coaxial waveguide system formed by inner and outer conducting cylindrical walls between which the E layer travels. We theorize that the beam forms azimuthal clumps due to the negative mass effect, and subsequently radiates as coherent synchrotron radiation. The radiation is seen at the end of the waveguide when the frequency of such radiation is above the cutoff frequency of the cylindrical waveguide system. Further-

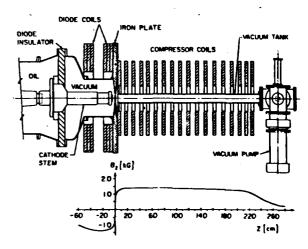


FIG. 1. Schematic of the University of Maryland rotating  $\boldsymbol{E}$  layer microwave generation system.

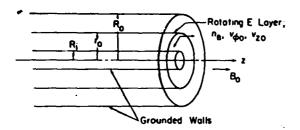


FIG. 2. Geometry of the model.

more, we expect an enhancement of radiation at frequencies associated with the various waveguide modes.

In this paper, a theoretical treatment identical in formalism to Sprangle<sup>13</sup> of the linear stability of a thin, dilute, rotating E layer propagating in a coaxial waveguide system is presented in Sec. II. Results of experimental studies of the radiation production in such a system are presented in Sec. III. Conclusions are drawn in Sec. IV.

#### II. THEORY

To study some of the properties associated with microwave generation from a rotating E layer traveling in a coaxial waveguide system, we consider the model whose geometry is shown in Fig. 2. The coaxial waveguide consists of ideal inner and outer concentric cylindrical conducting walls of radii  $R_i$  and  $R_0$ , respectively. The thin E layer of radius  $r_0$  is concentric with the conducting cylinders and has a mean azimuthal velocity  $v_{\phi 0} = \beta_{\phi 0} c$  and mean axial velocity  $v_{\phi 0} = \beta_{\phi 0} c$  and a relativistic mass ratio  $\gamma_0 = (1 - \beta_{\phi 0}^2 - \beta_{\phi 0}^2)^{-1/2}$ . The entire system is immersed in a uniform axial magnetic field  $B_0$ .

We examine the linear electromagnetic stability of this system in the limit of a tenuous beam at the condition for resonant interaction between a beam wave and the various TE and TM modes of the coaxial cylindrical waveguide. Such an interaction can be depicted as shown in Fig. 3, where a typical waveguide mode and beam mode are plotted in an  $\omega$ - $k_z$  diagram. At the interaction points indicated  $(k_z^+, \omega^-)$  and  $(k_z^+, \omega^+)$ , we have "resonant interaction". If these are both unstable, a backward  $(\omega^-)$  and forward  $(\omega^+)$  growing wave are produced. If no intersection of the two modes occurs, then a resonant interaction is not possible and the proceeding analysis will indicate no unstable wave. This is not to imply that only resonant interactions are unstable but to indicate the properties of such unstable interactions by analyzing the relatively simple resonant interaction.

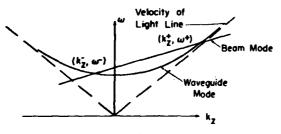


FIG. 3. Graphical description of resonant interaction between a waveguide mode and a beam mode.

The basic equations used in examining the linear electromagnetic stability of the system are the single particle orbit equations and Maxwell's equations. These equations are, respectively,

$$m\frac{d}{dt}\gamma\mathbf{v} = -e(\mathbf{E} + \mathbf{v} \times \mathbf{B}) \tag{4}$$

and

$$\left(\nabla^{2} - \frac{1}{c^{2}} \frac{\partial^{2}}{\partial t^{2}}\right) \mathbf{E} = \mu_{0} \frac{\partial \mathbf{J}}{\partial t} + \frac{1}{\epsilon_{0}} \nabla \rho, \tag{5a}$$

$$\left(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2}\right) \mathbf{B} = -\mu_0 \nabla \times \mathbf{J}, \tag{5b}$$

where m, -e are the rest mass and charge of a beam electron,  $\gamma = (1 - \beta_r^2 - \beta_\phi^2 - \beta_z^2)^{-1/2}$  is the relativistic mass ratio with  $v_r = \beta_r c = \dot{r}$ ,  $v_\phi = \beta_\phi c = r\dot{\phi}$ ,  $v_z = \beta_z c = \dot{z}$  as the velocity components in cylindrical coordinates,  $(r, \phi, z)$ , E, B are the electric and magnetic fields in the system, and  $\rho$ , J are the beam charge and current densities.

The equilibrium steady-state system is described mathematically by the conditions  $\partial/\partial t$ ,  $\partial/\partial \phi$ ,  $\partial/\partial z = 0$ . Under these conditions, plus the assumption of a tenuous beam, that is, the beam self fields are ignorable, Eq. (4) gives the beam equilibrium properties as

$$v_{\bullet} \equiv v_{\bullet 0} = 0,$$

$$v_{\bullet} \equiv v_{\bullet 0} = (eB_0/m\gamma_0)r_0 = \Omega_0 r_0/\gamma_0 = \omega_c r_0,$$

$$v_z \equiv v_{s0},$$
(6)

and

$$\gamma \equiv \gamma_0 = (1 - \beta_0^2)^{-1/2} = (1 - \beta_{\phi 0}^2 - \beta_{z0}^2)^{-1/2}$$

where  $B_0$  is the uniform applied axial magnetic field. We further assume that the beam is thin such that the beam density is given by  $n_b = n_s \delta(r - r_0)$ , where  $n_s$  is the surface particle density of the beam. Thus our system is a thin, tenuous rotating E layer that also propagates along an applied magnetic field between two concentric coaxial conductors of radii  $R_s$ ,  $R_0$ , as shown in Fig. 2.

The stability of the system is examined by linearizing Eqs. (4) and (5). The orbit equation is linearized as

$$r = r_0 + r_1(\phi, z, t),$$

$$\phi = \phi_0 + (\Omega_0/\gamma_0)t + \phi_1(\phi, z, t),$$

$$z = z_0 + v_{x0}t + z_1(\phi, z, t),$$
(7)

where subscript "one" variables are assumed small compared to subscript "zero" (equilibrium) values. The linearized particle velocities become

$$v_{r1} = \dot{r}_1,$$
 $v_{\phi 1} = r_0 \dot{\phi}_1 + (\Omega_0 / \gamma_0) r_1,$ 
 $v_{r1} = \dot{z}_1.$ 
(8)

Linearizing the electric and magnetic fields as

$$\mathbf{E} = \delta \mathbf{E}(r, \phi, z, t),$$

$$\mathbf{B} = B_0 \hat{\mathbf{z}} + \delta \mathbf{B}(r, \phi, z, t),$$
(9)

Fourier decomposing in the  $\phi$ ,z,t coordinates as  $\exp i(l\phi + k_z z - \omega t)$ , the linearized particle positions become

$$\bar{r}_1 = \frac{e}{m\gamma_0 D_i^2} \left( \psi_i^2 \ \overline{\delta E_i} + i \psi_i \frac{\Omega_0}{\gamma_0} \ \overline{\delta E_\phi} + i \psi_i \frac{\Omega_0}{\gamma_0} \beta_{s0} c \ \overline{\delta B_i} - \psi_i^2 \beta_{s0} c \ \overline{\delta B_\phi} + \psi_i^2 \beta_{\phi 0} c \ \overline{\delta B_s} \right), \tag{10a}$$

$$r_0\widetilde{\phi}_1 = \frac{ie}{m\gamma_0D_i^2} \left[ -\psi_i \frac{\Omega_0}{\gamma_0} \overline{\delta E_r} - i \left( \frac{\psi_i^2}{\gamma_{\phi 0}^2} + \frac{\Omega_0^2}{\gamma_0^2} \beta_{\phi 0}^2 \right) \overline{\delta E_\phi} + i\beta_{\phi 0}\beta_{s0} \left( \psi_i^2 - \frac{\Omega_0^2}{\gamma_0^2} \right) \overline{\delta E_s} \right]$$

$$-i\beta_{s0}c\psi_{i}^{2}\overline{\delta B_{r}}+\psi_{i}\frac{\Omega_{0}}{\gamma_{0}}\beta_{s0}c\overline{\delta B_{\phi}}-\psi_{i}\frac{\Omega_{0}}{\gamma_{0}}\beta_{\phi 0}c\overline{\delta B_{z}}\right],\tag{10b}$$

$$\tilde{z}_1 = (e/m\gamma_0\psi_1^2)(\overline{\delta E_x}/\gamma_{x0}^2 - \beta_{x0}\beta_{\phi 0}\overline{\delta E_{\phi}} - \beta_{\phi 0}c\overline{\delta B_r}),$$
(10c)

$$D_i^2 = \psi_i^2(\psi_i^2 - \Omega_0^2/\gamma_0^2), \quad \psi_i = \omega - l\Omega_0/\gamma_0 - k_z v_{z0},$$
  
$$\gamma_{z0}^2 = (1 - \beta_{z0}^2)^{-1}, \quad \gamma_{z0}^2 = (1 - \beta_{z0}^2)^{-1},$$

and the variables with bar or tildes represent the Fourierdecomposed amplitude that depend on r. In the same way, the z component of the linearized Maxwell equations

$$\left(\frac{\partial^{2}}{\partial r^{2}} + \frac{1}{r} \frac{\partial}{\partial r} - \frac{l^{2}}{r^{2}} + \frac{\omega^{2}}{c^{2}} - k_{z}^{2}\right) \overline{\delta E_{z}}$$

$$= -i\mu_{0}\omega \overline{\delta J_{z}} + i\frac{k_{z}}{\epsilon_{0}} \overline{\delta \rho}, \qquad (11a)$$

$$\left(\frac{\partial^{2}}{\partial r^{2}} + \frac{1}{r} \frac{\partial}{\partial r} - \frac{l^{2}}{r^{2}} + \frac{\omega^{2}}{c^{2}} - k_{z}^{2}\right) \overline{\delta B_{z}}$$

$$= -\mu_{0} \left(\frac{1}{r} \frac{\partial}{\partial r} r \overline{\delta J_{\phi}} - \frac{il}{r} \overline{\delta J_{r}}\right), \qquad (11b)$$

where, with the aid of the continuity equation, the linearized charge and current densities are given by

$$\delta \rho = \tilde{\sigma}_1 \delta(r - r_0) + e n_z \delta'(r - r_0) \tilde{r}_1, \qquad (12a)$$

$$\delta \mathbf{J} = -e n_z \delta(\mathbf{r} - \mathbf{r}_0) \tilde{\mathbf{v}}_1 + \tilde{\sigma}_1 \delta(\mathbf{r} - \mathbf{r}_0) \mathbf{v}_0 + e n_z \delta'(\mathbf{r} - \mathbf{r}_0) \tilde{\mathbf{r}}_1 \mathbf{v}_0$$
with
(12b)

$$\tilde{\sigma}_1 = e n_s \left( \frac{\psi_I - l \Omega_0 / \gamma_0}{\psi_I} \frac{\tilde{r}_1}{r_0} + i l \widetilde{\phi}_1 + i k_z \tilde{z}_1 \right). \tag{13}$$

In our analysis, we apply the continuity equation for the prescribed particle motion, whereas in Ref. 13 an independent charge conservation relationship is derived. This difference first appears in Eq. (13) where our coefficient of  $\bar{r}_1/r_0$  is replaced by "1" in the Ref. 13 analysis. In the final results for growth rates [Eqs. (21) and (28)], this effect appears in the terms  $(1-l^2/x_{ln}^2)^{1/3}$  and  $(1-l^2/y_{ln}^2)^{1/3}$ , respectively. We find that this factor is not substantial.

The linearized velocity components after Fourier decomposition are

$$v_{r1} \rightarrow -i\psi_{l}\tilde{r}_{l},$$

$$v_{\phi 1} \rightarrow -i\psi_{l}r\tilde{\phi}_{1} + \frac{\Omega_{0}}{\gamma_{0}}\tilde{r}_{1},$$

$$v_{s} \rightarrow -i\psi_{s}\tilde{r}_{s}.$$
(14)

Our procedure for solving these linearized equations is as follows. We assume the perturbed fields are the various

TE and TM coaxial waveguide fields, Fourier decomposed. We substitute these fields into both sides of Eq. (11), multiply the equation by the axial component of the field and by rdr, and then integrate from  $R_i$  to  $R_0$  to obtain a modified dispersion relation to the empty waveguide due to the presence of the tenuous beam. The following analytical results are obtained.

#### A. TE coaxial mode

The fields for the TE coaxial waveguide can be determined from the B, field with  $E_* = 0$ . This field is given by

$$\delta B_z = \mathcal{C}_l(\alpha_{ln} \mathbf{r}/\mathbf{R}_0) \exp(l\phi + k_z z - \omega t), \qquad (15)$$

where

$$\mathscr{C}_{i}(\alpha_{in}r/R_{0}) = CJ_{i}(\alpha_{in}r/R_{0}) + DN_{i}(\alpha_{in}r/R_{0}), \qquad (16)$$

 $J_{i}N_{i}$  are Bessel functions of first and second kind and  $(\alpha_{ln}/R_0)^2 = \omega^2/c^2 - k_z^2$ . Applying appropriate boundary conditions leads to a determination of the eigenvalues  $\alpha_{ln}$ . given by the solution to

$$J_i'(\alpha_{in})N_i'(\alpha_{in}R_i/R_0) - J_i'(\alpha_{in}R_i/R_0)N_i'(\alpha_{in}) = 0.$$
 (17)

Thus for each l, n = 1, 2, ..., which represents a radial mode number. Using Eq. (15), computing the other TE fields,  $E_r, E_{\phi}, B_r, B_{\phi}$ , and performing the manipulations as outlined above, the following modified dispersion relation is

$$\omega^{2} - k_{z}^{2} c^{2} - \alpha_{ln}^{2} c^{2} / R_{0}^{2} = (2\omega_{b}^{2} / \gamma_{0} D_{i}^{2}) \epsilon_{ln}^{2} [\overline{A}_{ln} \mathcal{E}_{i}^{2}(x_{ln}) + \overline{B}_{ln} \mathcal{E}_{i}(x_{ln}) \mathcal{E}_{i}(x_{ln}) + \overline{C}_{ln} \mathcal{E}_{i}^{2}(x_{ln})],$$
(18)

$$\begin{aligned}
\hat{\epsilon}_{in}^{2} &= \left[ \eta_{0}^{2} (1 - l^{2} / x_{in}^{2} \eta_{0}^{2}) \mathcal{C}_{i}^{2} (x_{in} \eta_{0}) \right. \\
&- \eta_{i}^{2} (1 - l^{2} / x_{in}^{2} \eta_{i}^{2}) \mathcal{C}_{i}^{2} (x_{in} \eta_{i}) \right]^{-1}, \\
\bar{A}_{in} &= \left[ x_{in} \psi_{i} \left( \frac{\Omega_{0}}{\gamma_{0}} - l \frac{\omega - k_{z} v_{z_{0}}}{x_{in}^{2}} \right) \right]^{2}, \\
\bar{B}_{in} &= 2 x_{in} \psi_{i} \frac{\Omega_{0}}{\gamma_{0}} \left( \frac{\Omega_{0}}{\gamma_{0}} - l \frac{\omega - k_{z} v_{z_{0}}}{x_{in}^{2}} \right) \\
&\times \left( \omega - k_{z} v_{z_{0}} - \frac{1}{2} \frac{l \Omega_{0}}{\gamma_{0}} \right), \end{aligned} \tag{19}$$

 $-l\frac{\Omega_0}{\gamma_0}\left(\frac{\Omega_0}{\gamma_0}\right)^2(\omega-k_z v_{s0}),$ 

 $\omega_h^2 = e^2 n_e / m \epsilon_0 r_0 \eta_0 = R_0 / r_0 \eta_i = R_i / r_0 x_{in} = \alpha_{in} r_0 / R_0$ 

For the specific case of resonant beam-waveguide mode interaction, mathematically given by

$$\omega \simeq \omega_0 = l\Omega_0/\gamma_0 + k_z v_{z0} = (k_z^2 c^2 + \alpha_{ln}^2 c^2/R_0^2)^{1/2}$$
, (20) the above dispersion relation can be solved for a growth rate  $\Gamma_{TE} = \int m\omega$ . The result is

$$\frac{\Gamma_{\text{TE}}}{\omega_{c} (\nu/\gamma_{0})^{1/3}} = \frac{\sqrt{3}}{(2\beta_{\phi 0})^{2/3}} \left(\frac{\Omega_{0}/\gamma_{0}}{\omega_{0}}\right)^{1/3} \times \left[ |g_{ln}^{\text{TE}}| \left(1 - \frac{l^{2}}{x_{ln}^{2}}\right) \right]^{1/3}, \tag{21}$$

where

$$g_{in}^{TE} = -\frac{\pi}{2} x_{in}^{3} \left[ J_{i}^{\prime} \left( \alpha_{ln} \frac{R_{i}}{R_{0}} \right) N_{i}^{\prime} (x_{ln}) - J_{i}^{\prime} (x_{ln}) N_{i}^{\prime} \left( \alpha_{ln} \frac{R_{i}}{R_{0}} \right) \right] \left[ J_{i}^{\prime} (\alpha_{ln}) N_{i}^{\prime} (x_{ln}) - J_{i}^{\prime} (x_{ln}) N_{i}^{\prime} (\alpha_{ln}) \right] \times \left\{ \frac{R_{0}}{r_{0}} \left[ J_{i}^{\prime\prime} (\alpha_{ln}) N_{i}^{\prime} \left( \alpha_{ln} \frac{R_{i}}{R_{0}} \right) - N_{i}^{\prime\prime} (\alpha_{ln}) J_{i}^{\prime} \left( \alpha_{ln} \frac{R_{i}}{R_{0}} \right) \right] - \frac{R_{i}}{r_{0}} \left[ J_{i}^{\prime\prime} \left( \alpha_{ln} \frac{R_{i}}{R_{0}} \right) N_{i}^{\prime} (\alpha_{ln}) - N_{i}^{\prime\prime} \left( \alpha_{ln} \frac{R_{i}}{R_{0}} \right) J_{i}^{\prime} (\alpha_{ln}) \right] \right\}^{-1},$$
(22)

and at resonance, we have

$$\omega_{0} = \frac{l\Omega_{0}}{\gamma_{0}} \gamma_{s0}^{2} \pm \beta_{s0} \gamma_{s0} \left[ \left( l \frac{\Omega_{0}}{\gamma_{0}} \gamma_{s0} \right)^{2} - \alpha_{ln}^{2} \frac{c^{2}}{R_{0}^{2}} \right]^{1/2}, (23)$$

$$k_{z}c = \frac{l\Omega_{0}}{\gamma_{0}} \gamma_{s0}^{2} \beta_{s0} \pm \gamma_{s0} \left[ \left( l \frac{\Omega_{0}}{\gamma_{0}} \gamma_{s0} \right)^{2} - \alpha_{ln}^{2} \frac{c^{2}}{R_{0}^{2}} \right]^{1/2},$$

and

$$v/\gamma_0 = \omega_h^2 r_0^2/2\gamma_0 c^2.$$

From Eq. (23), we require for resonance that  $l\beta_{\phi 0}\gamma_{z0} > x_{ln}$ .

#### B. TM coaxial mode

The fields for the TM coaxial waveguide modes can be determined from the  $E_z$  field with  $B_z = 0$ . This field is given

bу

$$E_z = \mathcal{C}_l(\beta_{ln}r/R_0) \exp(l\phi + k_z z - \omega t), \qquad (24)$$

where  $\mathcal{C}_i$  has the same form as in Eq. (16). Applying the appropriate boundary conditions allows the determination of the eigenvalues  $\beta_{in}$ , given by the solution to

$$J_{i}(\beta_{in})N_{i}(\beta_{in}R_{i}/R_{0}) - N_{i}(\beta_{in})J_{i}(\beta_{in}R_{i}/R_{0}) = 0,$$
 (25)

with

$$(\beta_{ln}/R_0)^2 = \omega^2/c^2 - k_z^2$$

Proceeding as in the TE mode, the following modified dispersion relation is obtained:

$$\omega^{2} - k_{z}^{2}c^{2} - \beta_{ln}^{2} \frac{c^{2}}{R_{z}^{2}} = \frac{2\omega_{b}^{2}}{\gamma_{c}D_{z}^{2}} (\omega\beta_{zo} - k_{z}c)^{2}\delta_{ln}^{2} \left[ A_{ln} \mathcal{C}_{l}^{2}(y_{ln}) + B_{ln} \mathcal{C}_{l}(y_{ln}) \mathcal{C}_{ln}^{2}(y_{ln}) + C_{ln} \mathcal{C}_{l}^{2}(y_{ln}) \right], \tag{26}$$

where

$$\delta_{ln}^{2} = \left[ \eta_{0}^{2} y_{ln}^{2} \mathcal{C}_{l}^{2} (\eta_{0} y_{ln}) - \eta_{l}^{2} y_{ln}^{2} \mathcal{C}_{l}^{2} (\eta_{l} y_{ln}) \right]^{-1},$$

$$A_{ln} = l^{2} \left( \psi_{l}^{2} - \frac{\Omega_{0}^{2}}{\gamma_{0}^{2}} \right) + y_{ln}^{2} \left( \frac{\psi_{l}^{2}}{(\omega \beta_{s0} - k_{s} c)^{2}} - 1 \right) \left( \psi_{l}^{2} - \frac{\Omega_{0}^{2}}{\gamma_{0}^{2}} \right),$$

$$B_{ln} = -y_{ln} l (\Omega_{0} / \gamma_{0}) \psi_{l},$$

$$C_{ln} = y_{ln}^{2} \psi_{l}^{2},$$
(27)

...ieh

$$y_{ln} = \beta_{ln} r_0 / R_0$$

For resonant beam-waveguide mode interaction, the above dispersion relation can be simplified and a growth rate  $\Gamma_{\text{TM}} \equiv Im\omega$  computed:

$$\frac{\Gamma_{\text{TM}}}{\omega_c (\nu/\gamma_0)^{1/3}} = \frac{\sqrt{3}}{(2\beta_{\phi 0})^{2/3}} \left( \frac{[I(\Omega_0/\gamma_0)\gamma_{s0})]^2 - \beta_{In}^2 c^2/R_0^2}{(\Omega_0/\gamma_0)\omega_0\gamma_{s0}^2} \right)^{1/3} \left[ h_{In}^{\text{TM}} \left( 1 - \frac{I^2}{y_{In}^2} \right) \right]^{1/3}, \tag{28}$$

where

$$\begin{split} h_{ln}^{\mathsf{TM}} &= \frac{\pi}{2} y_{ln} \bigg[ J_{l} \bigg( \beta_{ln} \, \frac{R_{i}}{R_{0}} \bigg) N_{l} (y_{ln}) - N_{l} \bigg( \beta_{ln} \, \frac{R_{i}}{R_{0}} \bigg) J_{l} (y_{ln}) \bigg] \big[ J_{l} (\beta_{ln}) N_{l} (y_{ln}) - J_{l} (y_{ln}) N_{l} (\beta_{ln}) \big] \\ &\times \bigg\{ \frac{R_{0}}{r_{0}} \bigg[ J_{l}' (\beta_{ln}) N_{l} \bigg( \beta_{ln} \, \frac{R_{i}}{R_{0}} \bigg) - N_{l}' (\beta_{ln}) J_{l} \bigg( \beta_{ln} \, \frac{R_{i}}{R_{0}} \bigg) \bigg] - \frac{R_{i}}{r_{0}} \bigg[ J_{l} \bigg( \beta_{ln} \, \frac{R_{i}}{R_{0}} \bigg) N_{l} (\beta_{ln}) - N_{l}' \bigg( \beta_{ln} \, \frac{R_{i}}{R_{0}} \bigg) J_{l} (\beta_{ln}) \bigg] \bigg\}^{-1} \end{split}$$

(29)

and at resonance

$$\omega \simeq \omega_{0} = l \frac{\Omega_{0}}{\gamma_{0}} \gamma_{so}^{2} \pm \beta_{so} \gamma_{so} \left[ \left( l \frac{\Omega_{0}}{\gamma_{0}} \gamma_{so} \right)^{2} - \beta_{ln}^{2} \frac{c^{2}}{R_{0}^{2}} \right]^{1/2},$$

$$k_{z}c = l \frac{\Omega_{0}}{\gamma_{0}} \beta_{so} \gamma_{so}^{2} \pm \gamma_{so} \left[ \left( l \frac{\Omega_{0}}{\gamma_{0}} \gamma_{so} \right)^{2} - \beta_{ln}^{2} \frac{c^{2}}{R_{0}^{2}} \right]^{1/2},$$
(30)

and for resonance to occur, we require  $l\beta_{\neq 0} \gamma_{z0} > y_{in}$ .

In Figs. 4-12, graphical resuts are presented of the linear growth rates for the waveguide-beam mode resonant interactions as given in Eqs. (21) and (28) as a function of various beam and system parameters. We find that an inner conductor for given beam properties and fixed outer conductor radius has very little effect unless the inner conductor is extremely close to the beam. With this in mind, we first present results for a hollow waveguide and show the growth rate dependence on harmonic number l, outer wall radius  $R_0$ , and axial beam velocity  $\beta_{20}$ . We specifically display the results as a function of frequency over the spectrum examined in the experiment, i.e., X and Ka bands. Finally, we display the effects of the inner conductor. We normalize our growth rates to  $\omega_c (v/\gamma_0)^{1/3} = (eB_0/m\gamma_0)(v/\gamma_0)^{1/3}$ . Thus, for a given  $\gamma_0$  and beam radius  $r_0$ , we see that as  $\beta_{r0}$  varies,  $B_0$  varies appropriately according to Eq. (6). However, for the range of  $\beta_{x0}$  covered in our graphs, there is very little change in  $B_0$ , i.e., about 30 G out of 1680 G.

In Figs. 4-6, the results of the TE resonant interaction, Eq. (21), are presented for a hollow waveguide  $R_c = 0$  as a

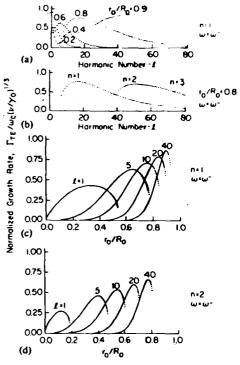


FIG. 4. Normalized TE growth rate [Eq. (21)] for beam properties  $\gamma_0 = 6$ ,  $\beta_{s0} = 0.2$ ,  $r_0 = 6$  cm, and  $R_1 = 0.0$  vs (a) harmonic number l for n = 1,  $\omega = \omega^-$  mode with  $r_0/R_0$  a parameter, (b) harmonic number l for  $r_0/R_0 = 0.8$ ,  $\omega = \omega^-$  mode with n a parameter, (c)  $r_0/R_0$  for n = 1,  $\omega = \omega^-$  mode with l a parameter, and (d)  $r_0/R_0$  for n = 2,  $\omega = \omega^-$  mode with l a parameter.

function of various system parameters. In Fig. 4, the beam properties are fixed at  $\gamma_0 = 6$ ,  $\beta_{s0} = 0.2$ , and  $r_0 = \dot{6}$  cm. In Fig. 4(a), the n = 1 growth rate is plotted versus harmonic number I with  $r_0/R_0$  as a parameter. We have only plotted the "backward" traveling wave  $(k, -, \omega^-)$ , as shown in Fig. 3. We see that for a given  $r_0/R_0$  there is no resonant interaction for low harmonic numbers. The interaction begins when  $l > x_{ln}/\beta_{\phi 0} \gamma_{s0}$ . However, once resonance can occur, the linear growth is fairly constant for beams near the outer wall for 1 < l < 80. In Fig. 4(b),  $r_0/R_0$  is fixed at 0.8 and all radial mode numbers are examined for stability in the region 1 < l < 80. We see that as the n = 1 mode growth rate falls at larger l, the n=2 radial mode becomes unstable for  $l \gtrsim 41$ , and finally at  $l \sim 75$ , the n = 1, 2, and 3 modes are all unstable. Thus we expect a fairly broad spectrum of unstable modes once the condition for the n = 1 mode is satisfied. In Figs. 4(c) and 4(d), the results are plotted versus  $r_0/R_0$  with harmonic number I a parameter. Again, the lack of resonance at low harmonic numbers is seen for beams located nearer to the outer wall.

In Figs. 5 and 6, the results are plotted as a function of frequency and specifically in the region from 0-20 and 20-40 GHz for comparison (qualitatively) with the experiment. In Fig. 5, the beam parameters are  $\gamma_0 = 6$ ,  $r_0 = 6$  cm,  $r_0/R_0 = 0.8$ , and  $\beta_{x0} = 0.0$ . For this case, we see that both the "forward" and "backward" unstable waves occur at exactly the same frequency; thus each point represents both the  $\omega^-$  and  $\omega^+$  growth rates. The entire unstable spectrum is shown in Fig. 5(a) where we see the first unstable mode is l = 7 for n = 1, l = 41 for n = 2, and l = 74 for n = 3. The frequency region covered by X band is shown in Fig. 5(b) and that by Ka band in Fig. 5(c). Only the n = 1 radial mode is

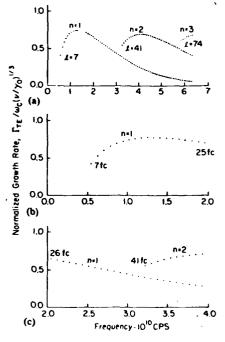


FIG. 5. Normalized TE growth rate [Eq. (21)] for beam properties  $\gamma_0 = 6$ ,  $\beta_{s0} = 0.0$ ,  $r_0 = 6$  cm,  $r_0/R_0 = 0.8$ ,  $R_1 = 0.0$  vs frequency. Note  $\omega^- = \omega^+$ . (a) Full spectrum for 1 < l < 80, (b) 0-20 GHz, and (c) 20-40 GHz.

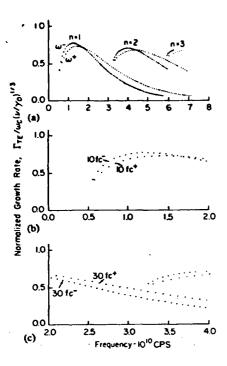


FIG. 6. Normalized TE growth rate [Eq. (21)] for beam properties  $\gamma_0=6$ ,  $\beta_{s0}=0.2$ ,  $r_0=6$  cm,  $r_0/R_0=0.8$ ,  $R_s=0.0$  vs frequency. Note  $\omega^-\neq\omega^+$ . (a) Full spectrum for 1<1<80, (b) 0-20 GHz, and (c) 20-40 GHz.

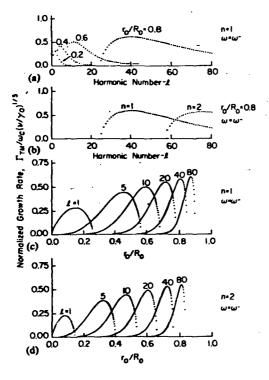


FIG. 7. Normalized TM growth rate [Eq. (28)] for beam properties  $\gamma_0 = 6$ ,  $\beta_{s0} = 0.2$ ,  $r_0 = 6$  cm, and  $R_i = 0.0$  vs (a) harmonic number l for n = 1,  $\omega = \omega^-$  mode with  $r_0/R_0$  a parameter, (b) harmonic number l for  $r_0/R_0 = 0.8$ ,  $\omega = \omega^-$  mode with n a parameter, (c)  $r_0/R_0$  for n = 1,  $\omega = \omega^-$  mode with l a parameter, and (d)  $r_0/R_0$  for n = 2,  $\omega = \omega^-$  mode with l a parameter.

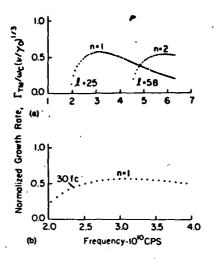


FIG. 8. Normalized TM growth rate [Eq. (28)] for beam properties  $\gamma_0=6$ ,  $\beta_{s0}=0.0$ ,  $r_0=6$  cm,  $r_0/R_0=0.8$ ,  $R_c=0.0$  vs frequency. Note  $\omega^-=\omega^+$ . (a) Full spectrum for 1< l<80 and (b) 20-40 GHz.

observed in the less than 20-GHz region while both the n=1 and n=2 radial modes are seen in the 20-40-GHz region.

In Fig. 6, the beam's axial velocity is  $\beta_{s0}=0.2$  while all other beam parameters remain the same as in Fig. 5. Now the  $\omega^-$  and  $\omega^+$  unstable modes are seen not to be coincident but are shifted below and above the  $l\omega_c$  frequency. Explicitly, the l=10 mode is labeled in Fig. 6(b) while the l=30 mode is labeled in Fig. 6(c). Thus, when  $\beta_{s0}=0$ , the points coalesce, whereas for finite  $\beta_{s0}$ , the two modes  $\omega^-$  and  $\omega^+$  separate with the separation becoming greater with larger

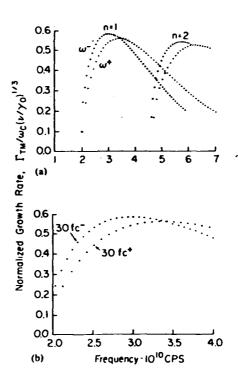


FIG. 9. Normalized TM growth rate [Eq. (28)] for beam properties  $\gamma_0 = 6$ ,  $\beta_{s0} = 0.2$ ,  $r_0 = 6$  cm,  $r_0/R_0 = 0.8$ ,  $R_1 = 0.0$  vs frequency. Note  $\omega^- \neq \omega^+$ . (a) Full spectrum for 1 < l < 80 and (b) 20–40 GHz.

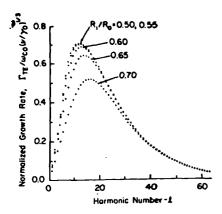


FIG. 10. Normalized TE growth rate [Eq. (21)] for beam properties  $\gamma_0 = 6$ ,  $\beta_{s0} = 0.2$ ,  $r_0 = 6$  cm,  $r_0/R_0 = 0.75$  vs harmonic number I for the n = 1,  $\omega = \omega^-$  mode with inner conductor radius a parameter,  $R_i/R_0$ . ( $\omega_{s0}$  is value of  $\omega_c$  when  $\beta_{s0} = 0.0$ .)

 $\beta_{ro}$ . We still may observe a strong interaction at a given frequency; however, from these results, they would have to be interpreted as different l numbers. As an example, in Fig. 6(c), we see the  $l = 30^-$  mode is very close to the  $l = 25^+$  mode, etc.

In Figs. 7-9, the results of the TM resonant interaction, Eq. (28), are presented for a hollow waveguide,  $R_i = 0$ . They are displayed in exactly the same format as the TE results. The most significant difference is that resonant interaction does not occur until larger harmonic numbers are reached, i.e., at higher frequencies for the same beam and conducting wall geometry. In fact, for  $r_0/R_0 = 0.8$ , no unstable modes are seen for less than about 20 GHz. The magnitude of the growth rates are the same as for the TE mode. In combining the results of the TE and TM resonant interaction, we would conclude that the less than 20-GHz spectrum involves unstable modes that are TE in nature and only the n = 1 radial mode, whereas the 20-40-GHz spectrum involves TE and TM modes with n = 1 and 2 for the TE waves and n = 1 for the TM waves. Including the effects of finite  $\beta_{s0}$ , we would

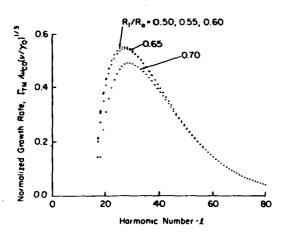


FIG. 11. Normalized TM growth rate [Eq. (28)] for beam properties  $\gamma_0=6$ ,  $\beta_{s0}=0.2$ ,  $r_0=6$  cm,  $r_0/R_0=0.75$  vs harmonic number I for the n=1,  $\omega=\omega^-$  mode with inner conductor radius a parameter,  $R_1/R_0$ . ( $\omega_{s0}$  is value of  $\omega_r$  when  $\beta_{s0}=0.0$ .)

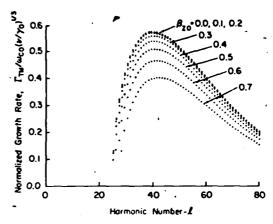


FIG. 12. Normalized TM growth rate [Eq. (28)] for beam properties  $\gamma_0 = 6$ ,  $r_0 = 6$  cm,  $r_0/R_0 = 0.75$ ,  $R_t/R_0 = 0.5$  vs harmonic number l for the n = 1,  $\omega = \omega^-$  mode with axial velocity  $\beta_{s0}$  a parameter. ( $\omega_{s0}$  is value of  $\omega_c$  when  $\beta_{s0} = 0.0$ .)

expect some discreteness in the power spectrum in the X-band frequency region but considerably less discreteness in the Ka-band frequency region.

In Figs. 10 and 11, the effects of an inner conductor on the TE and TM resonant interaction are shown. The beam parameters are  $\gamma_0 = 6$ ,  $r_0 = 6$  cm,  $\beta_{s0} = 0.2$ , and  $r_0/R_0 = 0.75$  in both figures. Also, only the results for the n = 1 and  $\omega^-$  mode are displayed. For the TE mode, Fig. 10, the hollow waveguide result is effectively obtained for  $R_i/R_0 \le 0.65$ , and substantial change is observed only when  $0.7 < R_i/R_0 < 0.75$ , that is, when the inner conductor is at the beam radius. For the TM mode, Fig. 11, the inner conductor has to be even closer before any substantial change is seen.

In Fig. 12, an appropriately normalized growth rate is plotted to show the effect of finite  $\beta_{s0}$ . Though there is a decrease in growth rate as  $\beta_{s0}$  increases, there is little change in the spectrum for the choice of system parameters chosen except as indicated above.

#### III. EXPERIMENT

The experiments were performed at the University of Maryland's Charged Particle Beam Facility. The apparatus used is shown schematically in Fig. 13. A coil pair forms the upstream half of a cusp magnetic field, and a solenoidal set of

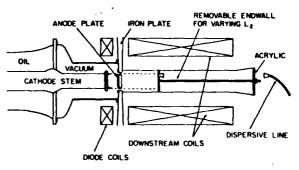


FIG. 13. General experimental configuration.

coils located around the downstream drift chamber provides the other half of the cusp. The solenoidal coils also provide a uniform field region where the beam propagates. Here beam modes couple with the modes of the hollow waveguide formed by the drift chamber. A soft iron plate has been inserted between these two coils to shorten the cusp field transition region.

In operation, a hollow cylindrical beam of 25-ns duration, full width at half-maximum (FWHM), is emitted from the circular knife-edge cathode of 6-cm radius. The cathode is made of tantilum or carbon. The electrons travel approximately 7.5 cm to a brass anode disc attached to the iron plate. The anode disc has an annular slit of 6-cm mean radius through which the electrons pass into the downstream region. During this transversal from the cathode to the downstream region, the electrons feel a  $v_2 \times B_r$ , force, which acts to convert the axial velocity of the beam electrons into rotational velocity, thereby producing a rotating ring of electrons. Some control over the amount of electrons propagating into the downstream region may be achieved by varying the annular slit width, while control over the energy of the particles may be achieved by varying the diode voltage.

Typical values used in the experiment were a diode voltage of 2.5 MV and a diode current of 10 kA. The magnetic field was varied over the range 800-1500 G. A vacuum of about  $10^{-5}$  Torr was maintained upstream and downstream of the cusp transition. The hollow rotating E layer propagating in the downstream region (typically, 2.5 MeV, 1-2 kA, 2-5 ns) is guided by the uniform magnetic field provided by the solenoidal coils. The chamber itself is a 3-m long, 15-cm diam aluminum cylinder, which forms the permanent outer conducting boundary for all experiments. Various inner conductors may be inserted into the downstream drift chamber on axis.

The radiated power spectrum for the experiment is obtained using the setup shown in Fig. 13. The downstream end of the drift chamber is flared to allow a smooth transition of TE and TM waveguide modes into free-space TEM modes. A pair of receiving horns and dispersive lines (X band, 7–12 GHz and Ka band, 24–40 GHz) of length 34 and 24 m, respectively, are placed a known distance beyond the acrylic endplate. Microwaves are transmitted through these lines through calibrated attenuators to calibrated detectors. The total radiation may be calculated by taking into account the solid angle subtended by the receiving horns and the attenuation curves for the dispersive lines. The frequency content may be determined from their dispersion characteristics.

#### A. Hollow guide experiments

The coupling of unstable beam modes into the TE and TM waveguide modes of an open-ended hollow cylindrical waveguide (15-cm diam) has been studied extensively. The total radiated power in X band has been measured as a function of applied cusp magnetic field, and is plotted in Fig. 14(a) for different injected beams with peak energies of 2.0 and 2.5 MV, respectively. Peak injected current in both cases is in the range of 1-2 kA. It is interesting to note that the

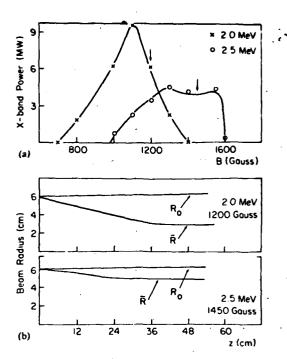


FIG. 14. (a) Radiated power in X-band (7-12 GHz) vs cusp magnetic field for two different peak electron beam energies. (b) Mean radius  $\vec{R}$  and outer radius  $R_0$  of the beam as a function of axial position downstream of the cusp.

cutoff of radiation occurs at higher applied magnetic fields for the higher energy cases, a result consistent with the fact that higher cusp fields are required, in this case, to prevent beam transmission through the cusp. <sup>16</sup> It is also evident that the highest radiated power is observed for the lower beam energy. The spectral content of this radiation is discussed in Sec. III.

Time integrated photographs of the light emitted when the downstream beam strikes a graphite-covered acrylic beamstop have been used to measure the mean beam radius  $\overline{R}$  and outer radius  $R_0$ , as a function of axial position in the drift chamber. Results of these studies for the 2.0- and 2.5-MeV cases are plotted in Fig. 14(b). The magnetic field was chosen so that the axial beam velocity in each case was approximately 0.3 c. It is readily seen that the loss of mean beam radius as the beam propagates is much greater in the 2.0-MeV case than in the 2.5-MeV case. This result is consistent with the higher power levels observed for the 2.0-MeV case. If the total loss in mean beam radius is due to radiated energy, the total radiated power should be about  $10^9$  W.

#### B. Effect of inner conducting boundaries

In order to study the effect of different conducting boundary systems on the radiated power, three different configurations were used. The conductors were inserted in the downstream drift chamber on axis. These were (1) a solid inner conductor of 5.0-cm-diam, (2) a solid inner conductor of 7.5-cm-diam, and (3) a 8.75-cm-diam "squirrel cage" conductor designed to allow image charge but not azimuthal image currents. Previous experiments have shown that such a configuration provides axial focusing of the beam elec-

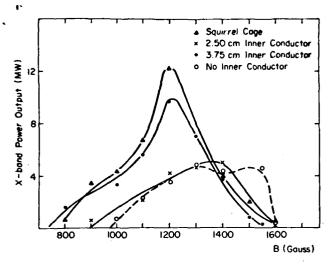


FIG. 15. Radiated power in X band for various conducting boundary configurations.

trons. 15 The total radiated power in X band has been measured as a function of applied cusp field for each of these configurations and is plotted in Fig. 15. It is evident that the highest radiated power levels are observed when an inner conductor is present and that larger diameter inner conductors seem to result in greater radiation production. Although the highest radiated powers are observed in the squirrel cage configuration, it is not clear from the results whether this is due to the changed boundary conditions or simply the larger diameter of the squirrel cage conductor.

#### C. Effects of preloaded azimuthal density structure

By passing the beam through an anode plate with a given number of azimuthally spaced transmission apertures located at the beam radius, a preloaded beam density structure may be imparted to the beam prior to the cusp field. In this manner, some control over the beam-waveguide mode coupling may be exercised. In the experiment, two anode plates, with  $l_A = 12$  and  $l_A = 40$  apertures, respectively, were used. As the electron cyclotron frequency is about 800 MHz in these experiments, the  $l_A = 12$  anode was chosen to maximize radiation in the X band while the  $l_A = 40$  anode was designed to maximize Ka-band radiation. The actual beam transmission area was 28% higher for the  $l_A = 12$  anode than for the  $l_A = 40$  anode. Typical power spectra and plots of the total power in each band as a function of applied magnetic field are shown in Figs. 16 and 17, respectively. Several features are apparent from these measurements.

(1) As expected, the radiated power in X band is greater for the  $l_A = 12$  case than for the  $l_A = 40$  case, while the radiated power in Ka band is greater for the  $l_A = 40$  case despite the reduced anode transmission area.

(2) While some control over the radiated power spectrum has been achieved, in both cases the greatest radiated power appears to be at frequencies between 12 and 24 GHz. This result is consistent with the theoretical studies that indicate that the TM modes do not occur for frequencies below about 16 GHz.

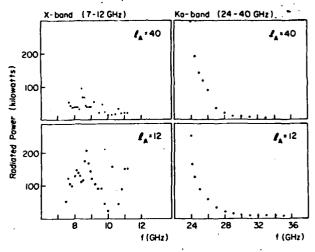


FIG. 16. Typical radiated power spectra in X band and Ka band for the  $I_A$  = 12 and  $I_A$  = 40 anodes.

(3) To exert greater control over the radiated power spectrum, it may be necessary to tailor the downstream waveguide towards the excitation of a particular mode.

#### D. Effect of finite axial length

In an attempt to fix the axial wavelength of the radiation and thereby control the radiated power spectrum, a movable conducting endwall was introduced into the system, as shown in Fig. 13. A small rectangular aperture in the endwall was used to couple radiation out of the fixed length cavity where it propagated to the end of the system guided by the 15-cm drift tube.

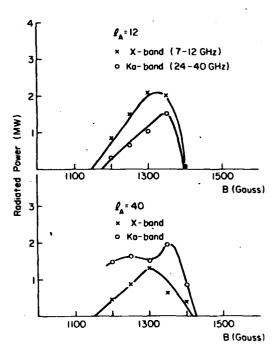


FIG. 17. Total radiated power in X band and Ka band vs cusp magnetic field for the  $I_A=12$  and  $I_A=40$  anodes.

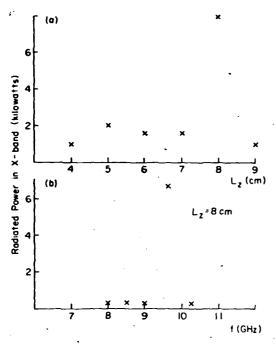


FIG. 18. Radiated power in X band for a finite length cylindrical drift chamber. (a) Radiated power vs axial length of the chamber. (b) Power spectrum at  $L_x = 8$  cm.

Total radiated power in the X band as a function of the axial cavity length  $L_z$  is plotted in Fig. 18(a). It is evident that radiated power is maximum at  $L_z = 8$  cm. The radiated output spectrum in X band is plotted for this case in Fig. 18(b). While further work remains to be done in this area, it is apparent that, by fixing the axial length of the system and thereby the axial wavelength of the cavity, individual modes may be excited. It is important to note, however, that total radiated power is much lower in this case, perhaps due to a relatively poor efficiency of coupling the radiation out of the system.

#### IV. CONCLUSIONS

The major conclusions to be drawn from this work are: (1) The theoretical analysis of possible resonant interactions

between beam modes and TE and TM waveguide modes of the drift chamber predicts a broadband radiation spectrum in reasonable agreement with experimental observations. (2) Experimental measurements of the radiation spectrum indicate that substantial radiated power is produced at frequencies in the range 12-24 GHz, a result consistent with the theoretical analysis, which shows that the TM modes should begin to be observed at about 16 GHz. (3) It is apparent that some control over the radiation spectrum may be achieved by either providing a preloaded azimuthal density structure to the beam or by using a finite length drift chamber to fix the axial wavelength of the radiation.

#### **ACKNOWLEDGMENTS**

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# High-power microwave generation from a rotating $\boldsymbol{\mathcal{E}}$ layer in a magnetrontype waveguide

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The generation of high-power bursts of microwave radiation from hollow, relativistic *E* layers injected through a cusped magnetic field into a magnetron-type conducting boundary configuration has been studied experimentally. Using a 2-MeV, 2-kA, 5-ns injected beam pulse, approximately 250 MW of radiated power have been generated at 9.6 GHz.

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The production of very high power bursts of microwave radiation by coupling the output of high-current relativistic electron accelerators to conventional microwave devices (klystrons, backward wave oscillators, and magnetrons) has been reported by several groups during the past few years. 1-5 Many of these experiments have reported conversion efficiencies of electron beam power to microwave power approaching those achieved in conventional devices working at much lower power levels. In this letter we report preliminary experimental results from a new type of microwave device that appears to have advantages with respect to conventional high-power magnetrons, and that has some features similar to our configuration. This new configuration also shares some features of its operation with gryrotrons, 6.7 although the electron orbits and conducting boundary systems of the two devices are quite different.

In a conventional multiresonator magnetron, electrons emitted from the cathode circulate around the device with EXB drift velocity, as shown in Fig. 1 (a). Radiation is produced by resonant interaction between the circulating space charge and the magnetron modes associated with the anode slow-wave structure. High power magnetrons 4.5 of this type have produced over 109 W of radiated power at about 4 GHz and have been designed around various operational limitations imposed by such systems. These include (i) the applied magnetic field being large enough to prevent electrons from crossing the anode-cathode gap (the Hull criterion<sup>8</sup>); (ii) the magnetic field being low enough to allow space-charge circulation at a drift velocity comparable to the phase velocity of the magnetron mode to be excited (the Buneman-Hartree condition9); (iii) the anode-cathode gap being small enough to allow field emission of electrons from the cathode in sufficient quantities to match the effective magnetron load impedance to the source impedance; and (iv) the high applied potentials in such systems being less than a value that would induce dc and rf breakdown. The result of these design requirements is that such devices do not appear to perform well at higher frequencies, in part because of the slow circulation velocity of the space charge and in part because electrical breakdown and other considerations limit the number of resonators that can be used to maximum of about eight.<sup>5</sup>

In our configuration [Fig. 1(b)], a rotating relativistic E layer is produced by passing a hollow nonrotating beam through a narrow symmetric magnetic cusp. The downstream chamber, in which the rotating beam propagates, has

a conducting wall structure that is similar to that of the magnetron. One again supposes that radiation is produced by resonant interaction of circulatory space charge and the various modes of the conducting chamber, but, in this case, the circulation is at the relativistic cyclotron frequency. Such a system may have a number of advantages over conventional magnetrons: (i) Much lower magnetic fields need be applied to operate at a given frequency, since the space-charge drift velocity is now given by  $r_0\omega_c$  where  $r_0$  is the the mean beam radius, and  $\omega_c$  is the relativistic cyclotron frequency (note that the Hull criterion does not apply here). (ii) The size of the device is not determined by diode impedance matching requirements and/or frequency selection considerations. (iii) There are no applied voltages in the interaction region and, therefore, less likelihood of dc and rf breakdown. As a result of all of the above, efficient higher frequency operation may be possible.

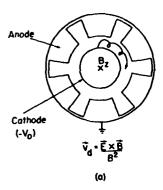
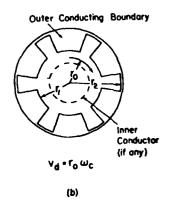


FIG. 1. (a) Conventional magnetron; (b) rotating E Layer in a magnetron-type waveguide.



The experimental configuration is shown schematically in Fig. 2. A hollow, nonrotating, relativistic electron beam (2 MeV, 20 kA, 30 ns) is emitted from a12-cm-diam circular knife-edge carbon cathode located 7.5 cm upstream of the anode. A 0.5-cm-wide circular slit in the anode plate allows a fraction of the diode current to pass through the anode plane into the magnetic cusp transition region, where  $v_* \times B_*$  force efficiently converts axial particle velocity to azimuthal velocity downstream of the cusp transition. The details of particle motion in the cusp region are reported elsewhere, 10 and it is easily shown that the downstream particle orbits are axis encircling with a gyroradius equal to the cathode radius. Typical downstream beam parameters are 2 MeV, 2 kA, and 5 ns, and the rotating E layer moves through the downstream region with an axial velocity in the range 0.1-0.3 c. The magnetic field upstream and downstream of the cusp transition is in the range 1200-1400 G, with a resultant relativistic cyclotron frequency of about 770 MHz at 1350 G.

The rotating electron beam in the region downstream of the cusp transition interacts with an outer conducting boundary of the type shown in Fig. 1(b) consisting of 12 resonators (n = 12) with dimensions  $r_1 = 6.5$  cm and  $r_2 = 7.5$ cm. No inner conducting boundary was used for these initial experiments. For comparison purposes, measurements were also made of the radiation produced when the beam interacts with a simple cylindrical outer conducting boundary of 7.5cm radius. Details of the radiation production in this latter configuration have been reported elsewhere. 11-13 Unlike a conventional magnetron, where radiation is usually extracted through a window in one of the resonators, radiation in this system was extracted axially out the downstream end of the drift chamber, as shown in Fig. 2. The downstream end of the drift chamber was flared to provide a smooth transition to free space, and the radiated power was detected by a receiving horn and a 34-m X-band (8-12 GHz) dispersive line connected to a calibrated attenuator and a calibrated detector. Total power was obtained by determining the effective radiation area at a given axial position of the receiving horn (by carefully surveying the region to determine over what area radiation is produced) from the output end of the drift chamber and multiplying the measured radiated power at the detector by the ratio of this area to that of the receiving horn. The power spectrum of the radiation was determined

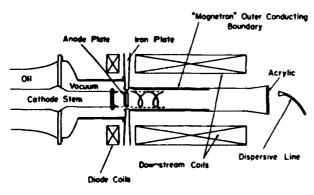
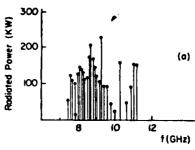


FIG. 2. General experimental configuration



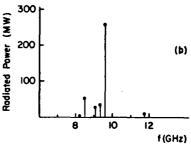


FIG. 3. Typical single shot power spectra for (a) simple cylindrical outer conducting boundary; (b) n=12 multiresonator magnetron outer conducting boundary. Applied magnetic field is 1350 G in each case.

by making use of the frequency-dependent group velocity of the radiation down the dispersive line. The undispersed radiation pulse duration was measured to be about 5 ns.

Results of these measurements are shown in Fig. 3, both for the simple cylindrical outer boundary and for the magnetron-type boundary. Each spectrum was obtained from a single shot, with each point representing a peak in the dispersed radiation waveform reaching the detector. The magnetic field setting in each case was 1350 G. Shot to shot reproducibility using the magnetron boundary was about  $\pm$  5% in frequency and about  $\pm$  20% in power amplitude. It is easily seen that both the total power and the spectrum of the emitted radiation are afected dramatically by the multiresonator boundary. For the simple outer boundary, the power is very broad band in the X-band frequency spectrum with peak powers around 200 kW. However, for the magnetron-type boundary, the peak power is a factor of 1000 greater and occurs predominantly at a single frequency around 9.6 GHz. A possible explanation for the strongly peaked spectrum that involves resonant interaction between a beam mode and the modes of the waveguide structure is that the magnetron-type boundary supports only the hollow smooth waveguide modes for which l = n, where l represents the azimuthal harmonic number of the beam. We would thus expect the radiation to an pear close to  $l\omega_c$ . For l=n=12,  $l\omega_c$  is around 9.2 GHz for a 1350-G applied field in close agreement with the frequency of the observed peak power. At this early state of examination, however, we cannot rule out the possibility that the boundary dramatically changes the mode structure and the interaction involves some other resonant interaction. Although the efficiency of the system (~10%) does not yet approach that of conventional magnetrons, the system is currently unoptimized, and further modifications may yield even higher radiated powers.

In conclusion, about 2×10<sup>8</sup> W of microwave radiation

at 9.6 GHz has been generated by the interaction of a 2-MeV, 2-kA, 5-ns cusp-generated rotating E layer with an n=12 multiresonator magnetron-type conducting boundary system. Such systems appear to overcome many of the operational limitations of conventional magnetrons and hold promise for efficient operation at higher frequencies.

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